



# DSSSB TGT

## PART(B)



# MATHS

## RIEMANN INTEGRATION

Part -2



08/10/2024 08:00 AM



1. The real part of  $e^{e^{i\theta}}$  is

$e^{e^{i\theta}}$  का वास्तविक भाग है

a)  $e^{\cos \theta} \cos \cos \theta$

b)  $e^{\cos \theta} \cos \sin \theta$

c)  $e^{\sin \theta} \cos \cos \theta$

d)  $e^{\sin \theta} \cos \sin \theta$



**2. Period of  $\coth x$  is**

**$\coth x$  की अवधि है**

**a)  $\frac{\pi}{2}i$**

**b)  $2\pi i$**

**c)  $\pi$**

**d) None of these**

**3. The value of  $\cosh^{-1}(\sqrt{5})$  is**

**$\cosh^{-1}(\sqrt{5})$  का मान है**

**a)**  $\log(\sqrt{5} + 2)$

**b)**  $\log(\sqrt{5} - 2)$

**c)**  $\log(\sqrt{2} + 5)$

**d)**  $\log(\sqrt{2} - 5)$

**4. Which one of the following is incorrect?**

**इनमें से कौन सा निम्नलिखित गलत है?**

**a)**  $\cosh \theta = \frac{e^{\theta} + e^{-\theta}}{2}$

**b)**  $\sin \theta = \frac{e^{i\theta} - e^{-i\theta}}{2i}$

 **c)**  $\sinh \theta = \frac{e^{i\theta} - e^{-i\theta}}{2}$

**d)**  $\cos \theta = \frac{e^{i\theta} + e^{-i\theta}}{2}$



**5.  $\cos(x + iy)$  is equal to**

**$\cos(x + iy)$  बराबर है**

**a)**  $\cos x \cos y - i \sin x \sin y$

**b)**  $\cos x \cosh y + i \sin x \sinh y$

 **c)**  $\cos x \cosh y - i \sin x \sinh y$

**d)**  $\cos x \cosh y - i \sin x \sin y$

6. The value of  $\sinh(\alpha + i\beta)$  is equal to

मान  $\sinh(\alpha + i\beta)$  का मान बराबर है

- a)  $\sinh \alpha \cos \beta - i \cosh \alpha \sin \beta$
- ✓ b)  $\sinh \alpha \cos \beta + i \cosh \alpha \sin \beta$
- c)  $\sin \alpha \cosh \beta + i \cos \alpha \sinh \beta$
- d)  $\sin \alpha \cosh \beta - i \cos \alpha \sinh \beta$

$$\sin(\alpha + i\beta)$$

$$\sinh \alpha \cdot \cosh(i\beta) + \cosh \alpha \cdot \sinh(i\beta)$$
$$\sinh \alpha \cos \beta + i \cosh \alpha \sin \beta$$

Notes

$$\sinh(ix) = i \sin x$$

$$\cosh(ix) = \cos x$$

$$\tanh(ix) = i \tan x$$



**7. Which one of the following is incorrect?**

**निम्न में से कौन सा गलत है?**

**a)**  $\operatorname{cosec}(ix) = -i \operatorname{cosech} x$

**b)**  $\tan(ix) = i \tanh x$

**c)**  $\sec(ix) = \operatorname{sech} x$

**✓d)**  $\cot(ix) = i \coth x$



**8. If  $\cos(x + iy) = k(\cos x + i \sin x)$ , then value of  $k \sin x$  is**

**यदि  $\cos(x + iy) = k(\cos x + i \sin x)$  है, तो  $k \sin x$  का मान है**

a)  $\cos x \cosh y$

b)  $-\cos x \cosh y$

☒ c)  $-\sin x \sinh y$

d)  $\sin x \sinh y$

$$\cos x \cdot \cos iy - \sin x \cdot \sin iy = k \cos x + i k \sin x$$

$$\downarrow$$
$$\cos x \cdot \cosh y - i \sin x \cdot \sinh y = k \cos x + i k \sin x$$

# # Notes

| Hyperbolic fun <sup>n</sup> | Domain               | Range                  |
|-----------------------------|----------------------|------------------------|
| $\sinh x$                   | $\mathbb{R}$         | $\mathbb{R}$           |
| $\cosh x$                   | $\mathbb{R}$         | $[1, \infty)$          |
| $\tanh x$                   | $\mathbb{R}$         | $(-1, 1)$              |
| $\coth x$                   | $\mathbb{R} - \{0\}$ | $\mathbb{R} - \{0\}$   |
| $\operatorname{sech} x$     | $\mathbb{R}$         | $(0, 1]$               |
| $\operatorname{cosech} x$   | $\mathbb{R} - \{0\}$ | $\mathbb{R} - [-1, 1]$ |



## #Inverse hyperbolic function

| Inverse hyperbolic fun <sup>n</sup> | Domain                 | Range                |
|-------------------------------------|------------------------|----------------------|
| $\sinh^{-1} x$                      | $\mathbb{R}$           | $\mathbb{R}$         |
| $\cosh^{-1} x$                      | $[1, \infty)$          | $(0, \infty)$        |
| $\tanh^{-1} x$                      | $(-1, 1)$              | $\mathbb{R}$         |
| $\coth^{-1} x$                      | $\mathbb{R} - \{0\}$   | $\mathbb{R} - \{0\}$ |
| $\operatorname{sech}^{-1} x$        | $(0, 1]$               | $[0, \infty)$        |
| $\operatorname{cosech}^{-1} x$      | $\mathbb{R} - [-1, 1]$ | $\mathbb{R} - \{0\}$ |

**9. Range of  $\operatorname{sech} x$  is**

**$\operatorname{sech} x$  की सीमा है**

**a)**  $(-1, 1) \longrightarrow \tanh x$

**b)**  $R - [-1, 1] \longrightarrow \operatorname{cosech} x$

**c)**  $R_0$

☒ **d)**  $(0, 1] \longrightarrow \operatorname{sech} x$



**10. Range of  $\coth^{-1} x$  is**

**$\cot h^{-1} x$  की सीमा है**

**a)  $(-1, 1]$**

**b)  $R$**

 **c)  $R_0$**

**d)  $[0, \infty)$**

For Practice



①. The Domain of fun<sup>n</sup>  $f(x) = \frac{1}{\sqrt{|x|-x}}$

(a)  $(0, \infty)$

(b)  $(-\infty, 0)$  ✓

(c)  $(-\infty, \infty)$

(d)  $(-\infty, \infty) - \{0\}$

$$|x| - x > 0$$

$$|x| > x$$

$$+ve$$

$$\pm \sqrt{x}$$

$$x \in (-\infty, 0)$$

Ques if  $f: \mathbb{R} \rightarrow \mathbb{R}$  is defined by  $f(x) = |x|$ .

(a)  $f'(x) = \frac{1}{|x|}$

(b)  $f'(x) = -x$

(c)  $f'(x) = \frac{1}{x}$

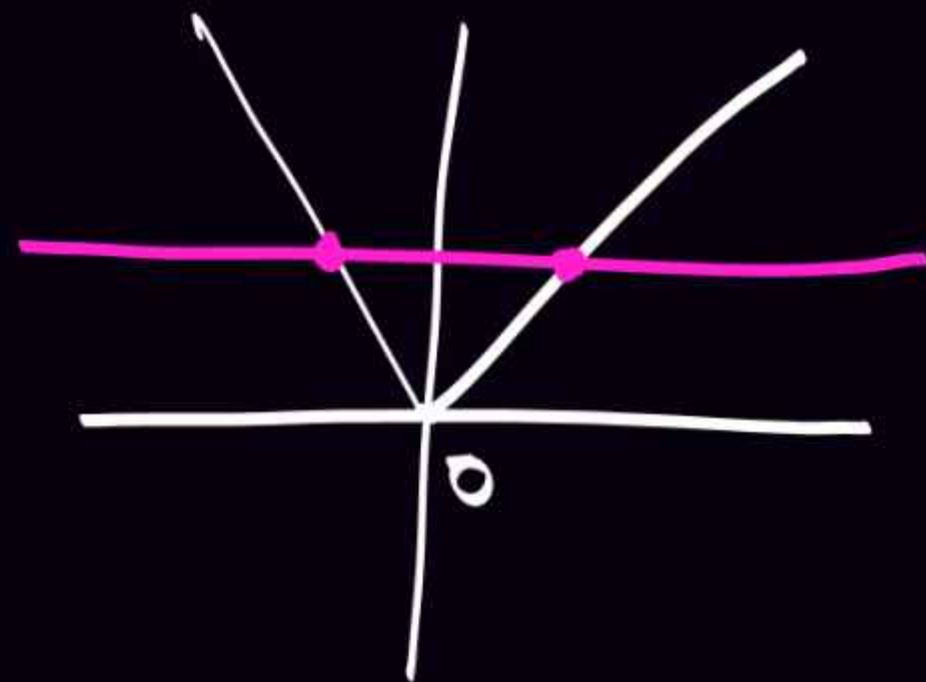
(d)  $f'(x)$  does not exist. ✓✓



one-one / onto.

एकैकी / आच्छादन.

many-one.



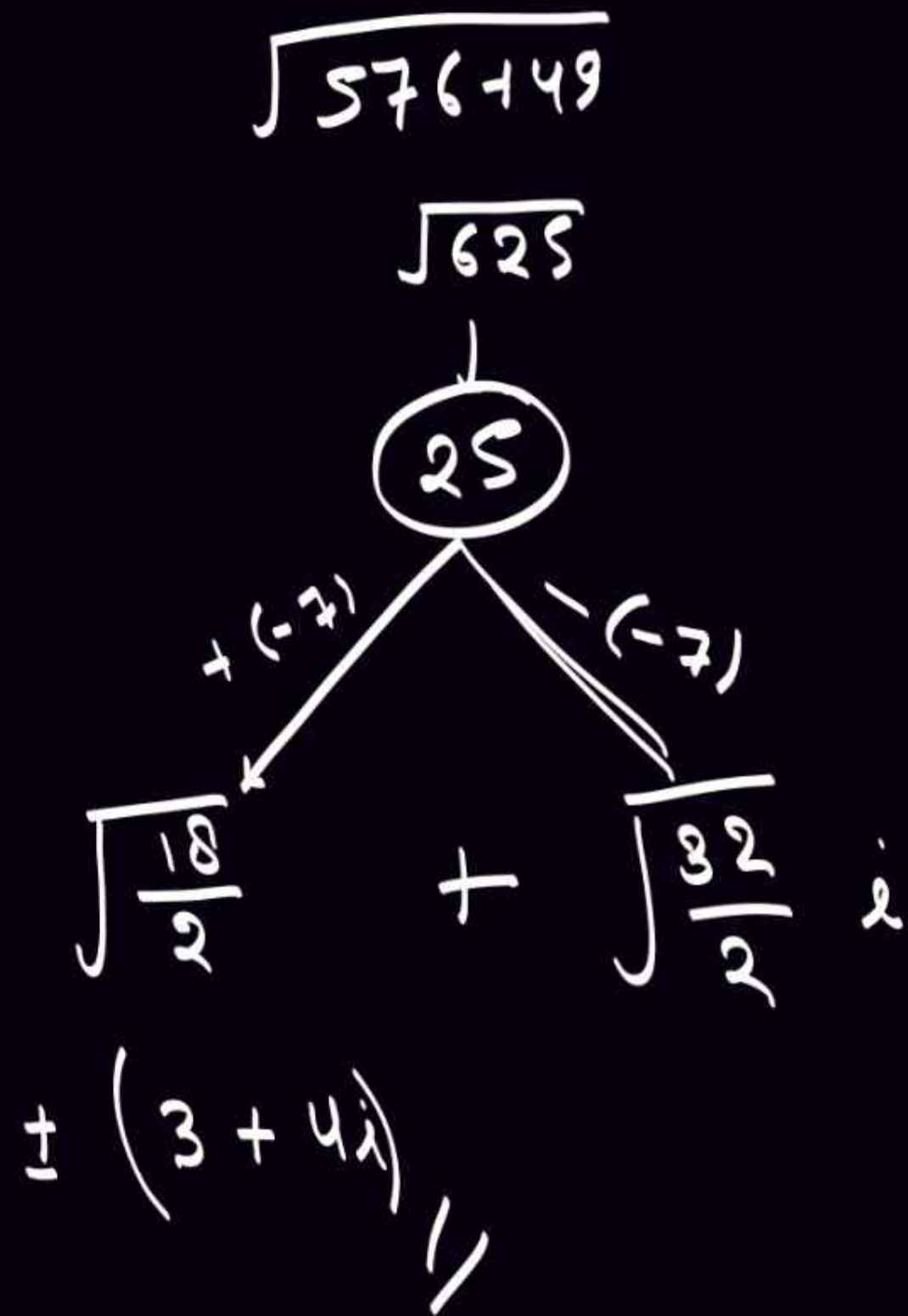
Ques Square root of  $-7 + 24i$ .

$$(9) \pm (-3+4i)$$

$$(b) \pm (4+3i)$$

$$(c) \pm (3 + 4i)$$

(d)  $\pm (-4 + 3i)$





Ques No of real root of the Equ<sup>n</sup>.

is.  $|x|^2 - 9|x| + 17 = 0.$

(a) 0

(b) 1

(c) 2

~~(d) 4.~~

↓  
 $x^2 - 9|x| + 17 = 0$

$\begin{array}{c} \textcircled{+} \\ \downarrow \\ 2 \end{array} + \begin{array}{c} \textcircled{+} \\ \downarrow \\ 2 \end{array} = 4$